#### A COURSE SYLLABUS - DOCTORAL SCHOOL

#### REGARDING THE QUALIFICATION CYCLE FROM 2023 TO 2027.

GENERAL INFORMATION ABOUT COURSE				
Course title	Doctoral Laboratory			
Name of the unit running the course	Doctoral School at the University of Rzeszów			
Type of course (obligatory, optional)	Obligatory			
Year and semester of studies	Year I-IV / Semester I-VIII			
Discipline	Mathematics			
Language of Course	Polish			
Name of Course coordinator	Prof. dr hab. Wiesław Śliwa			
Name of Course lecturer	Prof. dr hab. Wiesław Śliwa			
Prerequisites	Knowledge of mathematics at the master's level			

## BRIEF DESCRIPTION OF COURSE (100-200 words)

The doctoral thesis is aimed at preparing the doctoral student (under the substantive supervision of the supervisor) to independently conduct scientific research. It should also prepare the doctoral student to formulate research hypotheses, optimize research methodology, perceive and verbalize scientific problems scientific problems. The specific goal is: to perform research as part of the implementation of the doctorate, to analyze and develop the results of this research. The goal of the doctoral laboratory is also:

- expanding knowledge of methods of acquiring scientific information and preparing and writing scientific papers scientific work with respect for copyright and intellectual property,
- to draw the attention of the doctoral student to the need for further education and systematic familiarization with current scientific literature.

COURSE	LEARNING OUTCOMES AND MET	HODS OF EVALU	ATING LEARNING (	OUTCOMES
Learning outcome	The description of the learning outcome defined for the course  (Knows and understands)	Relation to the degree programme outcomes (symbol)	Learning Format (Lectures, classes,)	Method of assessment of learning outcomes (e.g. test, oral exam, written exam, project,)
(no.)				
1	World scientific achievements, including fundamentals, as well as general issues and selected specific issues - specific to the scientific discipline of mathematics.	P8S-WG1	laboratory	Project - implementation of the research plan
2	The main development trends of mathematics.	P8S-WG2	laboratory	Project - implementation of the research plan
3	Conceptual terminology resulting from scientific research in the discipline of mathematics and related disciplines in Polish and foreign languages recognized as leading for the discipline and related disciplines.	P8S-WG3	laboratory	Project - implementation of the research plan
4	The methodology of scientific research	P8S-WG4	laboratory	Project - implementation

		s of dissemination f scientific activition ode of open						of the research plan
Skills	(Able to)							
(no.)	ļ.,							
1	branches of creatively ic complex particular: - define the of scientific research hypresearch meresearch to apply	edge of various mathematics dentify and so problems; purpose and objected and creative the clusions based earch.	to lve in ect ate lop ues ely em,	P8S-UW1		labora	tory	Project - implementation of the research plan
2	Use scientific literature to identify and solve research problems.			P8S-UW/2		laboratory		Project - implementation of the research plan
3	Perform critical analysis and evaluate the results of research scientific research and their contribution to the advancement of knowledge.		and	P8S-UW <sub>3</sub>		labora	tory	Project - implementation of the research plan
Social	(Ready to)	<b>.</b>						
competence (no.)								
1	Critically evaluate the achievements within the discipline of scientific mathematics		P8S-KK1 labora		tory	Project - implementation of the research plan		
LEARNING FORMAT – NUMBER OF HOURS								
Semester	Lectures	Seminars	L	ab classes	Interr	nships	others	ECTS
(no.)	-	-		x 30 hrs. — 240 hrs.		-	-	24
				COLINICADI	LCTION		l	

#### **METHODS OF INSTRUCTION**

Discussion; critical analysis scientific literature; research; formulating of research problems and hypotheses; analysis of research results; preparation of doctoral dissertation

### **COURSE CONTENT**

The specifics of the research work, research techniques in mathematics are carried out in the period from semester I to semester VIII. Developing the concept and plan of the work, determining the purpose and methods of research.

Search for scientific literature on the research problem presented.

As part of the dissertation.

Analysis of the available literature on the subject matter of the dissertation.

Editing manuscripts with respect for the intellectual property of the authors.

The scientific literature used.

Preparation of the dissertation

#### **COURSE ASSESSMENT CRITERIA**

Credit for the course with a grade after each semester.

Implementation of scientific research. Presentation of own research results at seminars and scientific conferences. Preparation of manuscripts of scientific articles. Progress in the preparation of the dissertation. Possible semester grades are: 2.0, 3.0, 3.5, 4.0, 4.5, 5.0.

To obtain a passing grade, a conversion factor is applied for the corresponding percentage of points obtained:

- up to 50% insufficient, (the doctoral student does not make progress in scientific research, does not expand knowledge, does not study the readings, does not participate in substantive discussion, does not fulfill his/her academic obligations);
- 51% 60% sufficient, (the doctoral student makes negligible progress in scientific research, expands knowledge, studies primary literature, the discussion held is limited to a narrow range of substantive knowledge, fulfills basic scientific duties);
- 61% 70% sufficient plus, (the doctoral student makes progress in scientific research, expands knowledge, studies basic literature, substantively participates in the discussion, fulfills scientific duties);
- 71% 80% good, (doctoral student makes significant progress in scientific research, expands knowledge, studies primary and secondary literature, substantively participates in discussion, fulfills all scientific duties);
- 81% 90% good plus, (doctoral student makes significant progress in scientific research, systematically expands knowledge, studies primary and supplementary literature, substantively participates in discussions, fulfills of all scientific duties);
- 91% 100% very good (a doctoral student makes significant progress in scientific research, systematically expands knowledge, studies basic, complementary and beyond obligatory literature, substantively participates in discussion, fulfills all scientific duties)

## TOTAL PhD STUDENT WORKLOAD REQUIRED TO ACHIEVE THE INTENDED LEARNING OUTCOMES – NUMBER OF HOURS AND ECTS CREDITS

OUTCOMES - NOMBER OF HOORS AND ECTS CREDITS				
Activity	Number of hours			
Scheduled course contact hours	4 x 60 = 240			
Other contact hours involving the teacher (consultation hours, examinations)				
Non-contact hours – student's own work (preparation for classes or examinations, project, etc.)	4 × 120 - 480			
Total number of hours	720			
Total number of ECTS credits	24			
INCTRUCTION IN				

#### **INSTRUCTIONAL MATERIALS**

# Compulsory literature:

- 1. Tomkowicz, Grzegorz; Wagon, Stan The Banach-Tarski paradox. Second edition. Encyclopedia of Mathematics and its Applications, 163. Cambridge University Press, New York, 2016. xviii+348 pp.
- 2. Perez-Garcia, C.; Schikhof, W. H. Locally convex spaces over non-Archimedean valued fields. Cambridge Studies in Advanced Mathematics, 119. Cambridge University Press, Cambridge, 2010. xiv+472 pp.

- 3. Schikhof, W. H. Ultrametric calculus. An introduction to p-adic analysis. Cambridge Studies in Advanced Mathematics, 4. Cambridge University Press, Cambridge, 2006. xii+306 pp.
- 4. Schneider, Peter Nonarchimedean functional analysis. Springer Monographs in Mathematics. Springer-Verlag, Berlin, 2002. vi+156 pp.
- 5. Burillo, Josep Groups and the Banach-Tarski paradox. (Catalan) Butl. Soc. Catalana Mat. 23 (2008), no. 2, 181–199
- 6. Dougherty, Randall; Foreman, Matthew Banach-Tarski decompositions using sets with the property of Baire. J. Amer. Math. Soc. 7 (1994), no. 1, 75–124.
- 7. Dougherty, Randall; Foreman, Matthew Banach-Tarski paradox using pieces with the property of Baire. Proc. Nat. Acad. Sci. U.S.A. 89 (1992), no. 22, 10726–10728.
- 8. Banach, Stefan; Tarski, Alfred: Sur la décomposition des ensembles de points en parties respectivement congruentes, "Fundamenta Mathematicae" 6 (1924), s. 244–277.
- 9. Dekker, Th. J. Decompositions of sets and spaces. I, II. Nederl. Akad. Wetensch. Proc. Ser. A 59. Indag. Math. 18 (1956), 581–589, 590–595.
- 10. Tits, J. Free subgroups in linear groups. J. Algebra 20 (1972), 250–270.
- 11. Traina, Charles R. Trace polynomial for two-generator subgroups of SL(2,C). Proc. Amer. Math. Soc. 79 (1980), no. 3, 369–372.
- 12. Ershov, Mikhail; Golan, Gili; Sapir, Mark The Tarski numbers of groups. Adv. Math. 284 (2015), 21–53.

### Complementary literature:

- 1. Schneider, Peter p-adic Lie groups. Grundlehren der Mathematischen Wissenschaften. Springer, Heidelberg, 2011. xii+254 pp.
- 2. Lyndon, Roger; Schupp, Paul Combinatorial Group Theory. Classics in Mathematics. Springer-Verlag, Berlin, 2001. xiv+339 pp.
- 3. Lang, Serge Algebra. Graduate Texts in Mathematics. Springer-Verlag, New York, 2002. xvi+914 pp.
- 4. Engelking, Ryszard General Topology. Second Edition. Sigma Series in Pure Mathematics, Heldermann Verlag, Berlin, 1989. viii+529 pp.
- 5. Databases of scientific publications
- 6. Kolman R., Poradnik dla doktorantów i habilitantów. Oficyna Wydawnicza Ośrodka Postępu Organizacyjnego. , Bydgoszcz, 2000
- 7. Apanowicz J. Metodologiczne uwarunkowania pracy naukowej : prace doktorskie, prace habilitacyjne. warszawa : "Difin". 2005.
- 8. Stępień B. Zasady pisania tekstów naukowych : prace doktorskie i artykuły. Wydawnictwo Naukowe PWN. Warszawa. 2022.

\*(1 ECTS CREDIT CORRESPONDS TO 25 - 30 HOURS OF THE TOTAL WORKLOAD OF A DOCTORAL STUDENT, NEEDED TO ACHIEVE THE ESTABLISHED EFFECTS).

Date and signature of the Course lecturer
Approved by the Head of the Department or an authorised person