

SYLLABUS

REGARDING THE QUALIFICATION CYCLE FROM 2026 TO 2029
ACADEMIC YEAR 2027/2028

1. BASIC COURSE/MODULE INFORMATION

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|--|---|
| Course/Module title | Basic of Mathematical Statistics |
| Course/Module code * | |
| Faculty (name of the unit offering the field of study) | Faculty of Exact and Technical Sciences |
| Name of the unit running the course | Institute of Mathematics |
| Field of study | Mathematics |
| Qualification level | First-cycle studies (Bachelor's) |
| Profile | General academic |
| Study mode | Full-time |
| Year and semester of studies | Year 2, Semester 4 |
| Course type | Major subject |
| Language of instruction | English |
| Coordinator | Rostyslav Hryniv, PhD, DSc |
| Course instructor | Rostyslav Hryniv, PhD, DSc |

* - as agreed at the faculty

1.1. Learning format – number of hours and ECTS credits

| Semester (no.) | Lectures | Classes | Laboratories | Seminars | Practical classes | Internships | others | ECTS credits |
|-------------------|----------|---------|--------------|----------|----------------------|-------------|--------|-----------------|
| 4 | 15 | | 30 | | | | | 4 |

1.2. Course delivery methods

- conducted in a traditional way
 involving distance education methods and techniques

1.3. Course/Module assessment (exam, pass with a grade, pass without a grade)

Laboratory – pass with a grade

Lecture – pass without a grade

2. PREREQUISITES

Knowledge of basic concepts and facts from probability theory.

3. OBJECTIVES, LEARNING OUTCOMES, COURSE CONTENT, AND APPLIED TEACHING METHODS

3.1 Course/Module objectives

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|----|--|
| O1 | Familiarizing students with basic concepts, facts and methods in the field of descriptive statistics, parameter estimation and statistical hypothesis testing. |
| O2 | Developing students' ability to use methods of mathematical statistics to solve problems and interpret the obtained results. |

3.2 COURSE/MODULE LEARNING OUTCOMES (TO BE COMPLETED BY THE COORDINATOR)

| Learning Outcome | The description of the learning outcome defined for the course/module | Relation to the degree programme outcomes |
|------------------|---|---|
| LO_01 | The student knows basic concepts and facts from descriptive statistics, correlation analysis, parameter estimation and statistical hypothesis verification. | K_W01, K_W02, K_W03, K_W04 |
| LO_02 | The student is able to apply statistical methods to describe social, natural and technical phenomena. is able to apply the acquired knowledge to model analysis. | K_U01, K_U02 |
| LO_03 | The student is able to conduct simple statistical inference using concepts of mathematical statistics and utilizing it tools. | K_U13 |
| LO_04 | The student understands the importance of learned facts and methods of mathematical statistics in interpreting social, natural and economic phenomena. is able to critically evaluate information from various sources. | K_K01, K_K02, K_K03 |

3.3. Course content (to be completed by the coordinator)

A. Lectures

Content outline

1. Basic issues of statistical data analysis. Classification of variables. Measurement scales.
2. Empirical distribution of a trait and its description. Basic parameters of quantitative and qualitative traits. Measures of central tendency, positional measures and measures of dispersion.
3. Examining the dependence of two traits. Linear correlation coefficient (Pearson's). Rank correlation coefficients (Spearman's). Chi-square test of independence. Chuprov's, Cramer's and Pearson's coefficients for qualitative traits.
4. Foundations of estimation theory. Properties of estimators. Interval estimation. The problem of minimal sample size.
5. Testing statistical hypotheses. Parametric significance tests. Chi-square goodness-of-fit test.

B. Classes, laboratories, seminars, practical classes

Content outline

1. **Descriptive Statistics:** Calculating fundamental parameters of empirical distributions using raw data and frequency tables. Graphical representation of data distributions.
2. **Analysis of Quantitative Variables:** Constructing and interpreting correlation tables and marginal distributions. Calculating covariance and Pearson's linear correlation coefficient for bivariate data.
3. **Rank Correlation:** Calculating and interpreting non-parametric measures of association: Spearman's rho and Kendall's tau.
4. **Analysis of Qualitative Variables:** Testing independence between categorical variables using the Chi-square test. Calculating association coefficients (Chuprov's, Cramer's V, and Pearson's C) and interpreting the results.
5. **Estimation of the Mean:** Constructing confidence intervals for the population mean under various conditions: known variance, unknown variance, and unknown population distribution (large-sample approximations).
6. **Estimation of Variance and Proportions:** Constructing confidence intervals for the population variance and the population proportion (structure index).
7. **Sample Size Determination:** Calculating the minimum sample size required to achieve specific margins of error and confidence levels.
8. **Hypothesis Testing:** Formulating and executing statistical tests, including parametric significance tests and Chi-square goodness-of-fit tests.

3.4 . Methods of Instruction

Lecture: a problem-solving lecture/a lecture supported by a multimedia presentation/ distance learning

Laboratory classes: designing and conducting experiments

4. ASSESSMENT TECHNIQUES AND CRITERIA

4.1 Methods of evaluating learning outcomes

| Learning outcome | Methods of assessment of learning outcomes (e.g. test, oral exam, written exam, project, report, observation during classes) | Learning format (lectures, classes,...) |
|------------------|--|---|
| LO_01 | observation during classes, laboratory tasks, project | lecture, laboratory |
| LO_02 | observation during classes, laboratory tasks, project | lecture, laboratory |
| LO_03 | observation during classes, laboratory tasks, project | lecture, laboratory |
| LO_04 | observation during classes, laboratory tasks, project | lecture, laboratory |

4.2 Course assessment criteria

Passing the laboratory on the basis of laboratory tasks and activity during classes. The condition for passing the exercises is obtaining at least 50% of points from each laboratory task. The final grade is then determined according to the scale:

below 50% pts. – fail,

[50 – 60%] pts. – satisfactory,

[60 – 70%] pts. – satisfactory plus,

[70 – 80%] pts. – good,

[80 – 90%] pts. – good plus,

[90– 100%] pts. – very good.

Activity during exercises can raise the grade by at most half a degree.

Passing the lecture on the basis of a positive grade from a statistical data analysis project.

**5. Total student workload needed to achieve the intended learning outcomes
– number of hours and ECTS credits**

| Activity | Number of hours |
|--|-----------------|
| Course hours | 45 |
| Other contact hours involving the teacher (consultation hours, examinations) | 2 |
| Non-contact hours - student's own work (preparation for classes or examinations, projects, etc.) | 55 |
| Total number of hours | 102 |
| Total number of ECTS credits | 4 |

* One ECTS point corresponds to 25-30 hours of total student workload

6. Internships related to the course/module

| | |
|---------------------------------------|-----------------------|
| Number of hours | <i>Not applicable</i> |
| Internship regulations and procedures | <i>Not applicable</i> |

7. Instructional materials

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| <p>Compulsory literature:</p> <ol style="list-style-type: none"> 1. Casella, G., Berger, R. L. (2002). Statistical inference. CRC Press. 2. James, G., Witten, D., Hastie, T., Tibshirani, R. (2013). An introduction to statistical learning: with applications in R. Springer New York. https://doi.org/10.1007/978-1-4614-7138-7 |
| <p>Complementary literature:</p> <ol style="list-style-type: none"> 1. Agresti, A., Franklin, C., Klingenberg, B. (2022). Statistics: the art and science of learning from data. 5th ed. Pearson. 2. Dalgaard, P. (2008). Introductory statistics with R. 2nd ed. Springer New York. https://doi.org/10.1007/978-0-387-79054-1 |

Approved by the Head of the Department or an authorised person